

Year 12 Mathematics Specialist Units 3, 4 Test 6 2020

Calculator Assumed **Statistical Inference**

STUDENT'S NAME	

DATE: Thursday 10 September **TIME**: 50 minutes **MARKS**: 45

INSTRUCTIONS:

Standard Items: Pens, pencils, drawing templates, eraser

Special Items: Three calculators, notes on one side of a single A4 page (these notes to be handed in with this

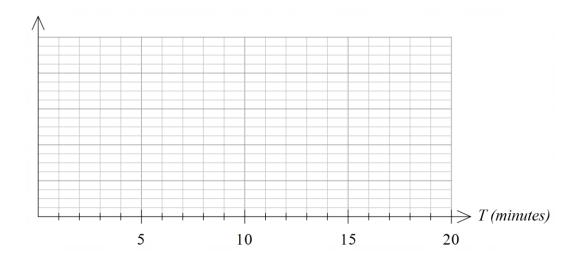
assessment)

Questions or parts of questions worth more than 2 marks require working to be shown to receive full marks.

1. (3 marks)

The time T in minutes that it takes a taxi to arrive is uniformly distributed with a population mean of $\mu(T) = 12$ and a population variance of $\sigma^2(T) = 81$.

If a large number of samples, each with a sample size of 16 times is taken, sketch the likely distribution of the sample mean \overline{T} below.



(6 m	(6 marks)		
Cons	Consider the following statement:		
	The 95% confidence interval for the mean ranges from 0.1 to 0.4.		
Dete	rmine, with reasons, if the following statements are TRUE or FALSE.		
(a)	The probability that the true mean is greater than 0 is at least 95%.	[2]	
(b)	There is a 95% probability that the true mean lies between 0.1 and 0.4.	[2]	
(c)	If we were to repeat the experiment over and over, then 95% of the time the true me falls between 0.1 and 0.4.	ean [2]	
	juns between 0.1 and 0.4.	[2]	

2.

((10 ma	arks)	
		cicket balls are weighed. It is known that the population mean $\mu = 163~g$ and the ation standard deviation $\sigma = 20~g$	
((a)	State the (approximate) distribution of the sample mean weight per cricket ball.	[3]
((b)	Determine the probability that the sample mean weight of a cricket ball will be more than $163.5g$.	[2]
,	Suppo	se that more than 100 cricket balls are weighed.	
((c)	How would this affect your answer to part (b)? Explain without recalculation.	[2]
	-	ports club desires that the probability that the sample mean will be between $163g$ and is greater than 45% .	
((d)	Determine the minimum number of cricket balls that will need to be weighed.	[3]

3.

4.	(9 marks)
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Matthew and Angus want to check the claim that a single Kitkat weights 17 g. They buy two packets that contain 18 Kitkats each, and weigh them both for a combined weight of 620 g. Matthew calculates the sample standard deviation to be s = 1.2 g and assumes that the weights of the Kitkats is uniformly distributed.

(a) Based on Matthew's data, obtain a 95% confidence interval for μ , the population mean weight of a Kitkat. [4]

Angus points out that the population distribution is not uniformly distributed but is normally distributed.

(b) How does this affect the confidence interval calculated in part (a)? [2]

A different sample of 36 Kitkats is taken and it is found that the sample standard deviation is $s = 0.9 \ g$. A confidence interval for the population mean weight is determined to be $16.92 \le \mu \le 17.48$.

(c) Determine the level of confidence, to the nearest 0.01%, used to calculate this interval.

[3]

5.	(9 marks)
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The cable for the new zip line on the Matagarup bridge is required to support a weight of 12 kN. A first random sample of n cables found the mean cable strength to be 12.5 kN. Repeated sampling of the mean indicated that the standard deviation of the sample means was 300 N.

(a) Determine a 90% confidence interval for the cable strength mean, correct to the nearest N. [3]

A second random sample of 4n cables found that the average cable strength was 12.3 kN. Assume that both samples were drawn from the same population.

(b) What is the standard deviation of the sample mean for the second sample, current to the nearest N [2]

Suppose that the first random sample and the second random sample are combined to produce a third random sample of 5n cables. Consider the 90% confidence intervals as:

Random Sample	Size	90% Confidence interval
First	n	A
Second	4 <i>n</i>	В
Third	5 <i>n</i>	С

(c) Which of the intervals, A, B or C, will provide the greatest precision in determining the population mean μ ? Justify your answer. [2]

(d) Which of the intervals, A, B or C, contains the true value of the population mean μ ?

Justify your answer. [2]

He ta	an wants to estimate the population mean height in metres, of the current year 12 cohorakes a random sample of 50 students and determines a 99% confidence interval for μ . I limit of this interval is 1.7929 m and the width of this interval is 0.0658 m.	
(a)	Determine the sample mean for this sample of 50 students.	[2]
(b)	Calculate, correct to 0.01 metres, the sample standard deviation for the sample of 50 students.	[3]

Declan knows that taller people have a greater chance to play basketball for the College. He knows from previous experience that in a group of 50 students, there is a 6.3% chance that this group has at least one student who plays basketball for the College with a standard deviation of 1.72. Declan decides to investigate this further and randomly samples groups of 50 students a total of 30 times.

(c) State the approximate distribution of the mean number of samples of 50 students who have at least one student that plays basketball for the College.

[3]